

(i) Printed Pages : 4 Roll No.

(ii) Questions : 8 Sub. Code :

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Exam. Code :

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B.A./B.Sc. (General) 1st Semester
(2122)

MATHEMATICS

Paper—III : Trigonometry & Matrices

Time Allowed : Three Hours] [Maximum Marks : 30

Note :—Attempt FIVE questions in all, selecting at least TWO questions from each unit.

UNIT—I

1. (a) By taking $z = \cos \theta + i \sin \theta$, in the identity

$$z + z^3 + z^5 + \dots + z^{2n-1} = \frac{z(1-z^{2n})}{1-z^2}, \text{ prove that}$$

$$(i) \cos \theta + \cos 3\theta + \cos 5\theta + \dots + \cos(2n-1)\theta = \frac{\sin 2n\theta}{2\sin \theta}$$

$$(ii) \sin \theta + \sin 3\theta + \sin 5\theta + \dots + \sin(2n-1)\theta = \frac{1 - \cos 2n\theta}{2\sin \theta}$$

3

(b) Show that each primitive 12th root of unity satisfies

$$x^4 - x^2 + 1 = 0. \quad 3$$

2. (a) Use De Moivre's theorem to solve
 $(4 + x)^5 - (4 - x)^5 = 0.$ 3
- (b) If $\tan(x + iy) = \cosh(\alpha + i\beta)$, prove that
 $\tanh\alpha \tan\beta = \operatorname{cosec} 2x \sinh 2y.$ 3
3. (a) For $z \in \mathbb{C}$, prove that
 $\cosh^{-1} z = 2n\pi i \pm \log(z + \sqrt{z^2 - 1}), n \in \mathbb{Z}.$ 3
- (b) If $\cosh^{-1}(x + iy) + \cosh^{-1}(x - iy) = \cosh^{-1}a$, show that
 $2(a - 1)x^2 + 2(a + 1)y^2 = a^2 - 1.$ 3
4. (a) Sum upto infinity the series
 $\frac{1}{2} \sin \alpha + \frac{1.3}{2.4} \sin 2\alpha + \frac{1.3.5}{2.4.6} \sin 3\alpha + \dots$ 3
- (b) Prove that $\lim_{x \rightarrow 0} \frac{1}{x^2} \log\left(\frac{\tan^{-1} x}{x}\right) = \frac{-1}{3}.$ 3

UNIT—II

5. (a) Show that every Hermitian matrix A can be uniquely expressed as $P + iQ$, where P and Q are real symmetric and real skew symmetric matrices respectively. Also show that A^0A is real iff $PQ = -QP.$ 3

- (b) Find the rank of the matrix $\begin{bmatrix} 1 & 3 & 1 & 3 \\ 2 & 8 & 5 & 10 \\ 1 & 7 & 7 & 11 \\ 3 & 11 & 7 & 15 \end{bmatrix}.$ 3

6. (a) Find non-singular matrices P and Q such that PAQ is

in normal form where $A = \begin{bmatrix} 2 & -1 & 3 & 4 \\ 0 & 3 & 4 & 1 \\ 2 & 3 & 7 & 5 \\ 2 & 5 & 11 & 6 \end{bmatrix}$ and hence

find the rank of A. 3

- (b) Discuss for all values of k, the system of equations

$$(3k - 8)x + 3y + 3z = 0$$

$$3x + (3k - 8)y + 3z = 0$$

$$3x + 3y + (3k - 8)z = 0$$

as regards the nature of solution. 3

7. (a) Solve the following system of equations, if consistent :

$$x + y - 2z + 4t = 5$$

$$2x + 2y - 3z + t = 3$$

$$3x + 3y - 4z - 2t = 1 \quad 3$$

- (b) Find the eigen values and the corresponding eigen vectors

of the matrix $\begin{bmatrix} 1 & 2 & 2 \\ 1 & 2 & -1 \\ -1 & 1 & 4 \end{bmatrix}$. 3

8. (a) Verify Cayley-Hamilton theorem for the matrix A and

hence find its inverse, $A = \begin{bmatrix} 1 & 3 & 7 \\ 4 & 2 & 3 \\ 0 & 2 & 1 \end{bmatrix}$. 3

(b) Let $A = \begin{bmatrix} 1 & 1 & 2 \\ -1 & 2 & 1 \\ 0 & 1 & 3 \end{bmatrix}$. Is A diagonalizable? If it is, then

find invertible matrix P such that $P^{-1}AP$ is a diagonal matrix. 3

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